

# Parallelization and benchmarks



# Gaussian DFT computational kernel

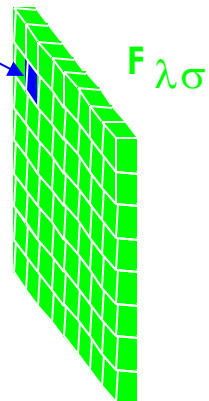
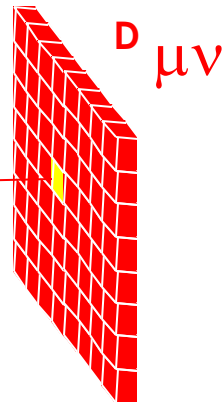
## Evaluation of XC potential matrix element

$$\rho(\mathbf{x}_Q) = \sum_{\mu\nu} \mathbf{D}_{\mu\nu} \chi_{\mu}(\mathbf{x}_Q) \chi_{\nu}(\mathbf{x}_Q)$$

$$\mathbf{F}_{\lambda\sigma} += \sum_Q \mathbf{w}_Q \chi_{\lambda}(\mathbf{x}_Q) \mathbf{V}^{\text{XC}}[\rho(\mathbf{x}_Q)] \chi_{\sigma}(\mathbf{x}_Q)$$

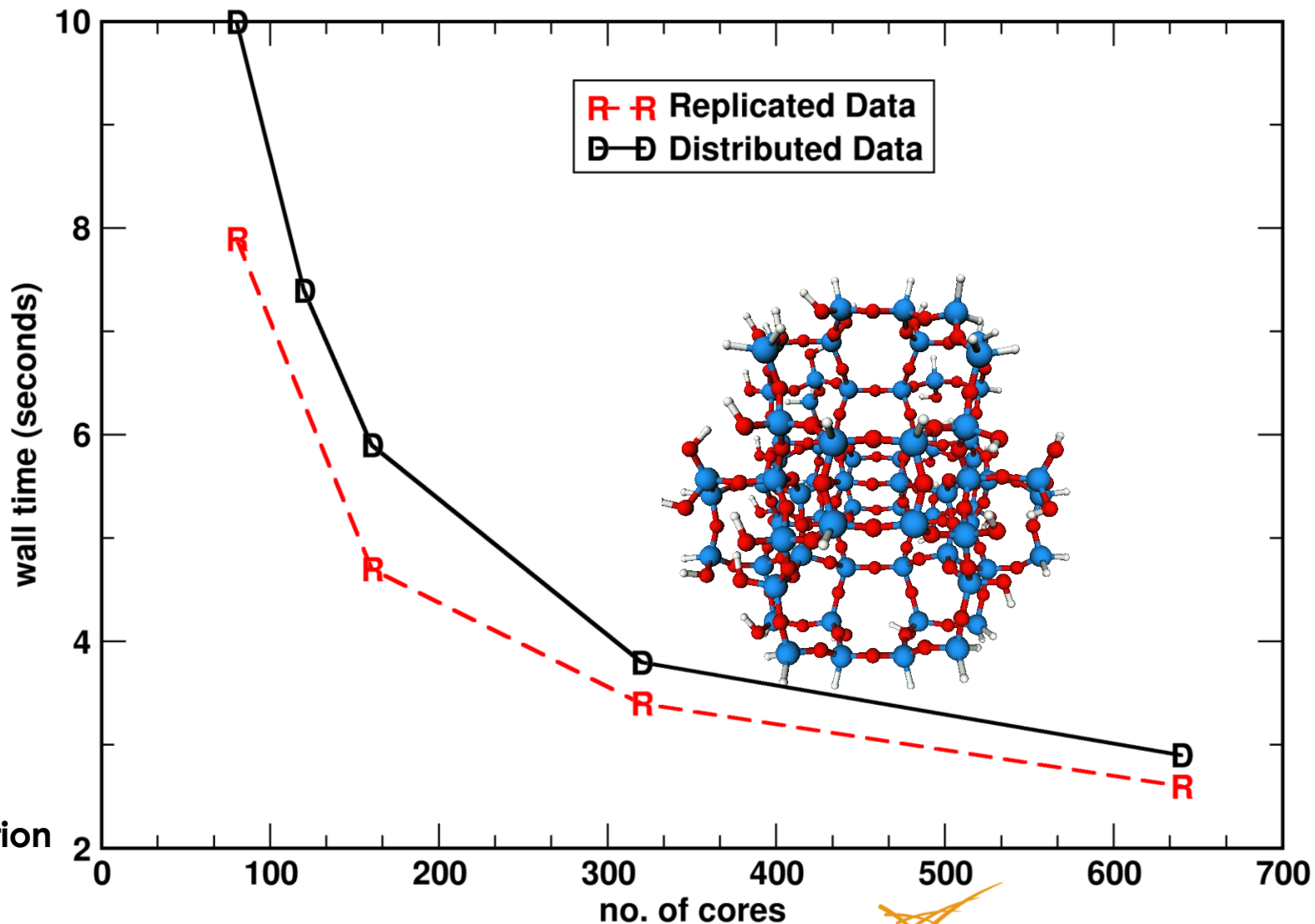
```

my_next_task = SharedCounter()
do i=1,max_i
  if(i.eq.my_next_task) then
    call ga_get()
    (do work)
    call ga_acc()
    my_next_task =
      SharedCounter()
  endif
enddo
barrier()
    
```



Both **GA operations** are greatly dependent on the communication **latency**

# Parallel scaling of the DFT code



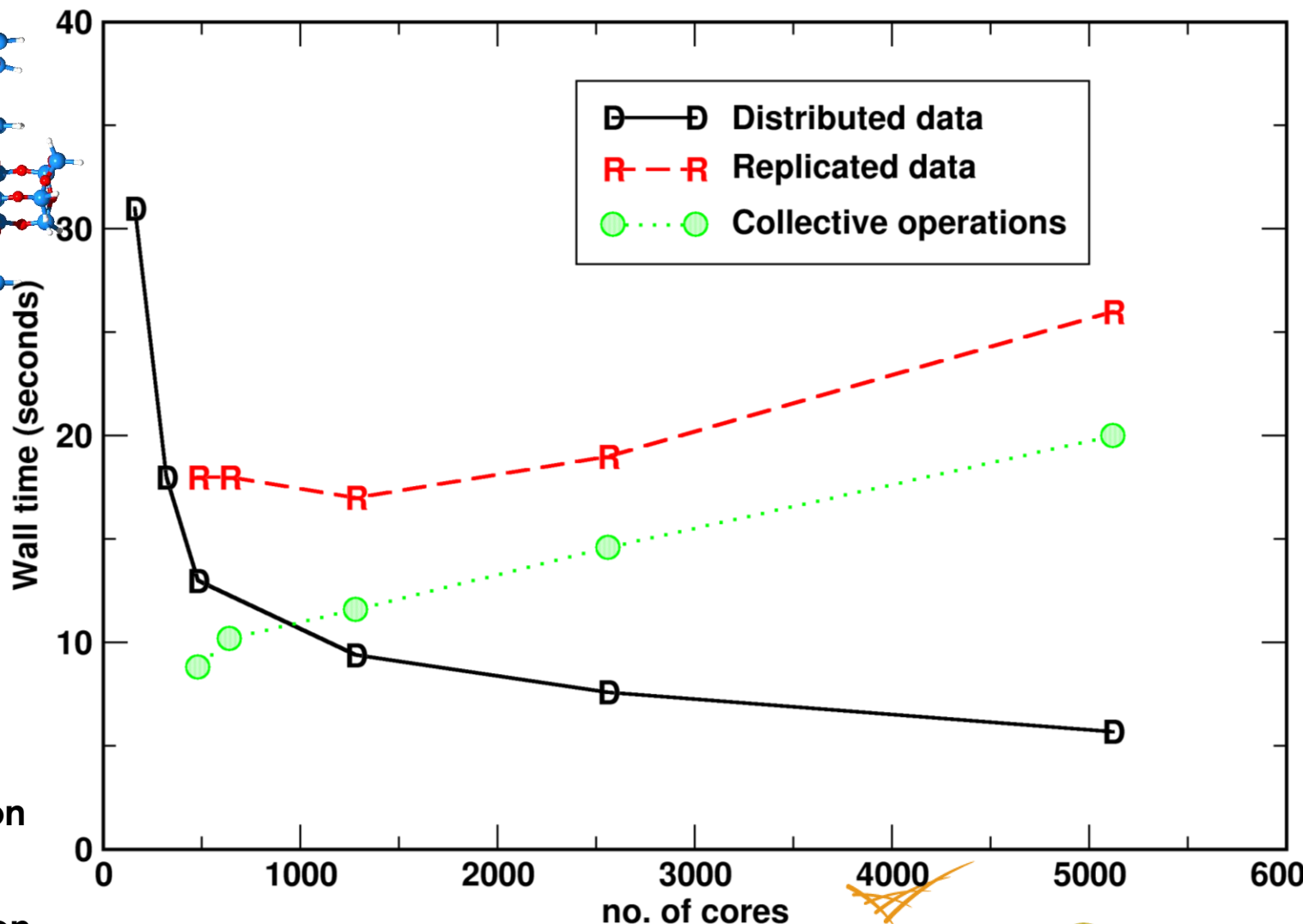
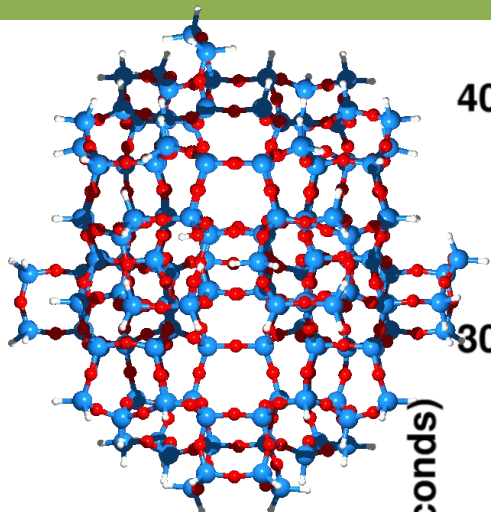
Si<sub>28</sub>O<sub>148</sub>H<sub>66</sub>

3554 Basis functions

LDA wavefunction  
XC build

Benchmark run on  
Cray XK6

# Parallel scaling of the DFT code



$\text{Si}_{159}\text{O}_{264}\text{H}_{110}$

7108 Basis functions

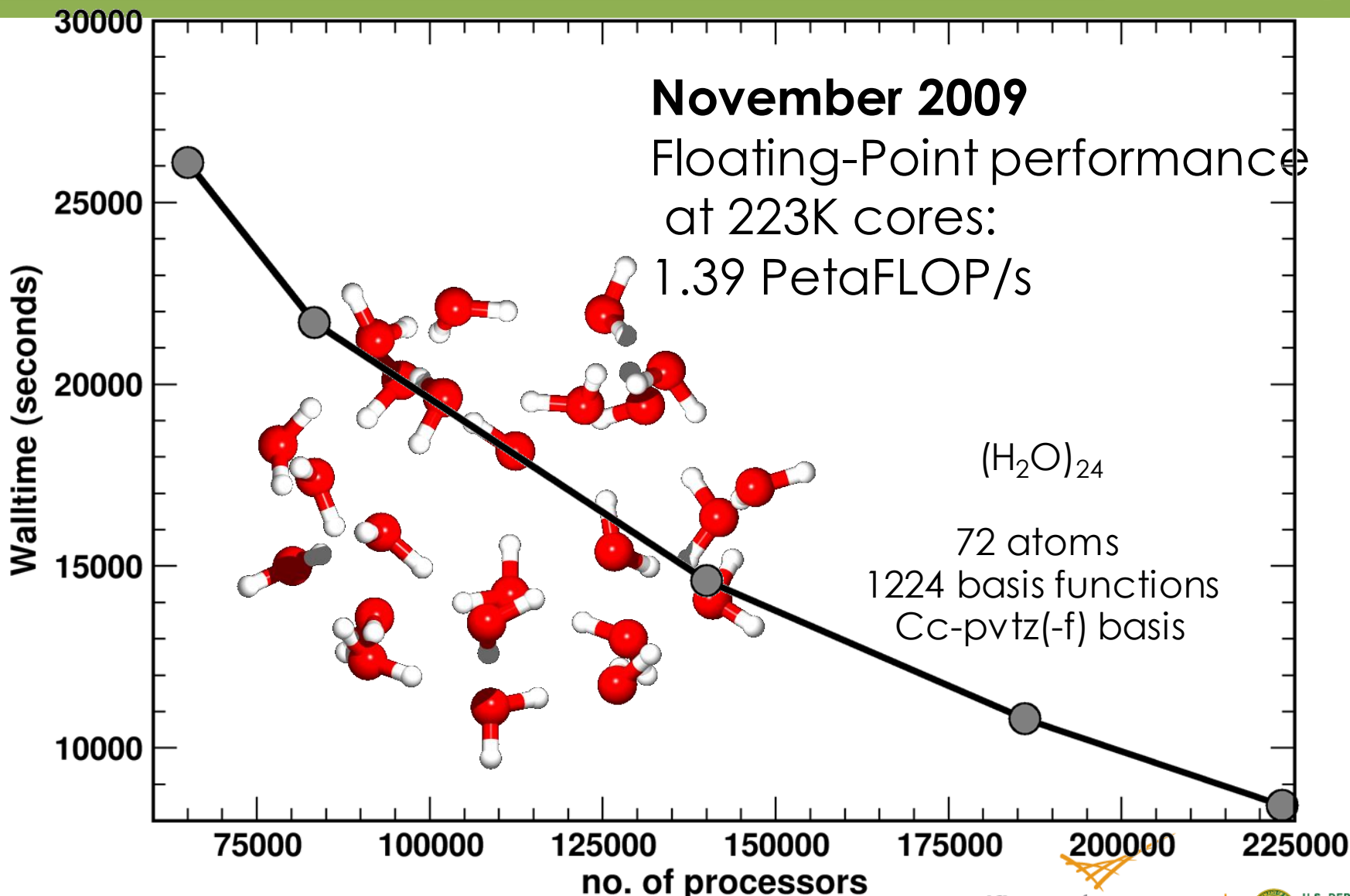
LDA wavefunction

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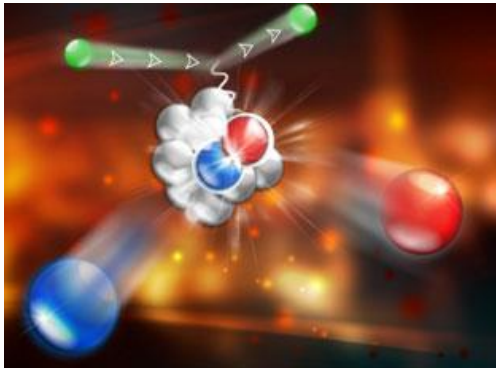
# CCSD(T) run on Cray XT5 : 24 water



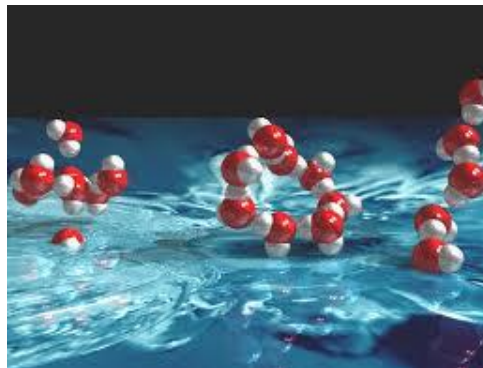
$$\hat{H}|\Psi(1,\dots,N)\rangle = E|\Psi(1,\dots,N)\rangle$$

## Many Particle Systems

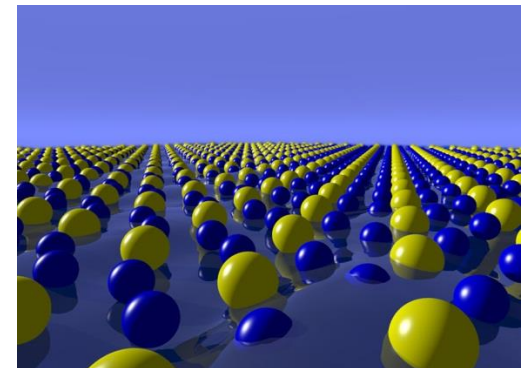
### Nuclear Physics



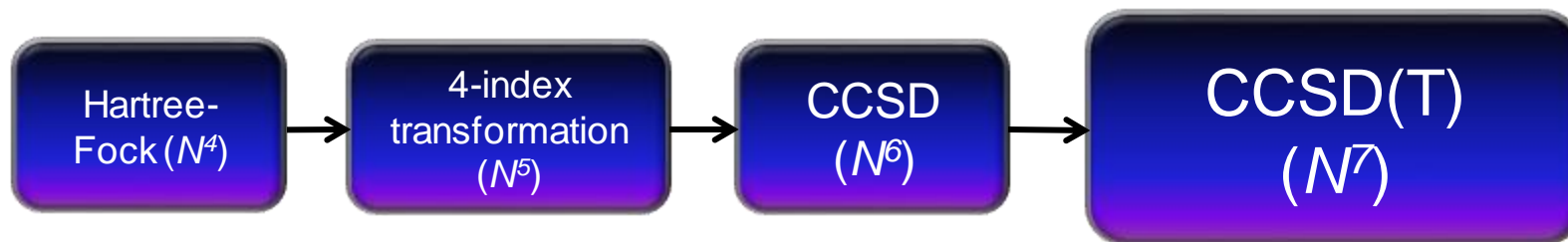
### Quantum Chemistry



### Solid State Physics

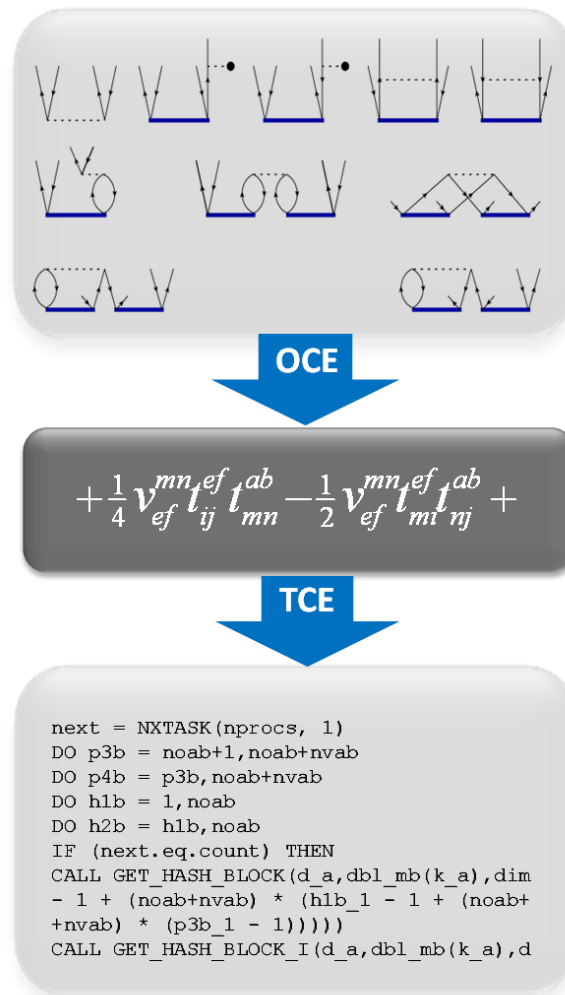


Method	Numerical complexity
CCSD (singles & doubles)	$N^6$
CCSD(T) (perturbative triples)	$N^7$
CCSDT (singles & doubles & triples)	$N^8$
CCSDTQ (singles & doubles & triples & quadruples)	$N^{10}$



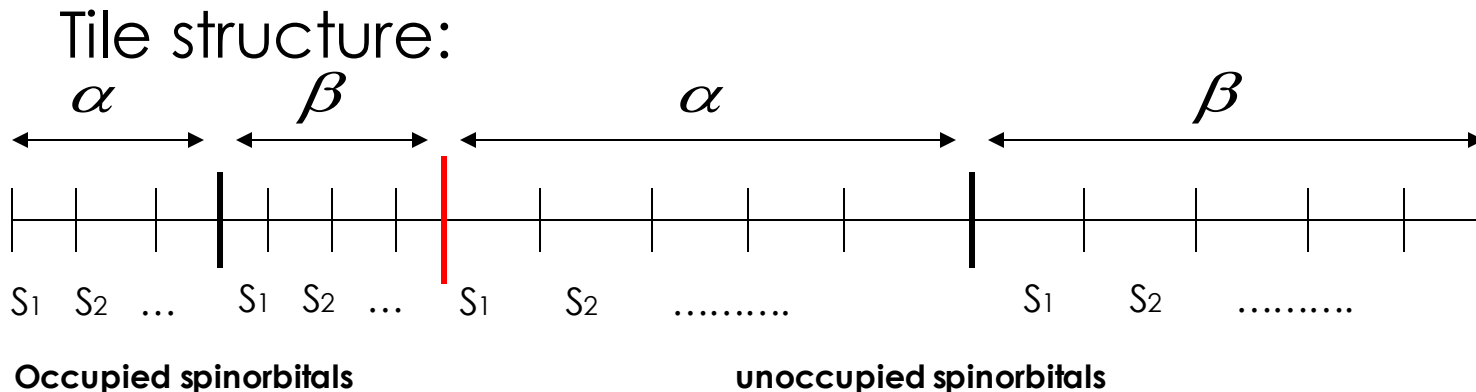
# What is Tensor Contraction Engine (TCE)

- Symbolic manipulation & program generator
  - ◆ Automates the derivation of complex working equations based on a well-defined second quantized many-electron theories
  - ◆ Synthesizing efficient parallel computer programs on the basis of these equations.
- Granularity of the parallel CC TCE codes is provided by the so-called tiles, which define the partitioning of the whole spinorbital domain.



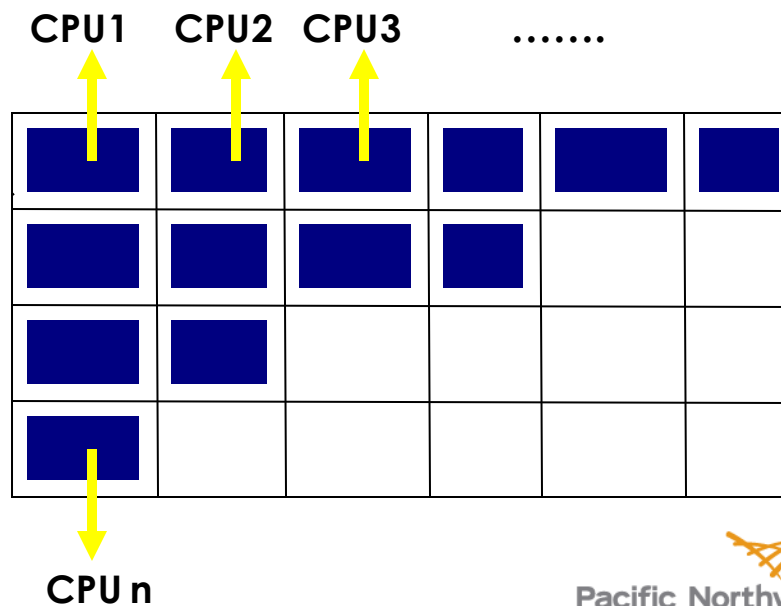


# What is Tensor Contraction Engine (TCE)

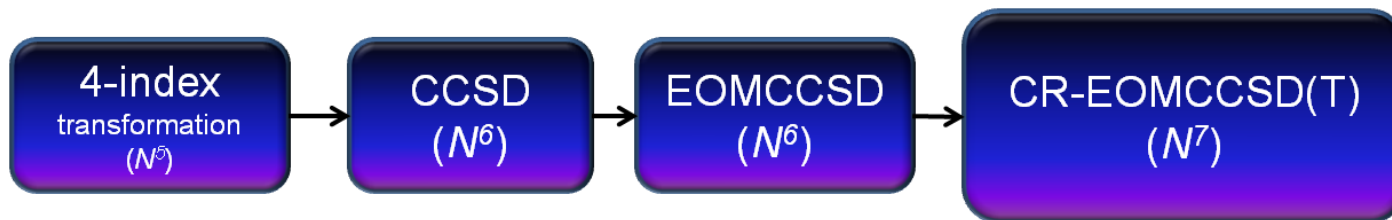


Tile-induced block structure of the CC tensors:

$$T_a^i \Rightarrow T_{[p_n]}^{[h_m]}$$



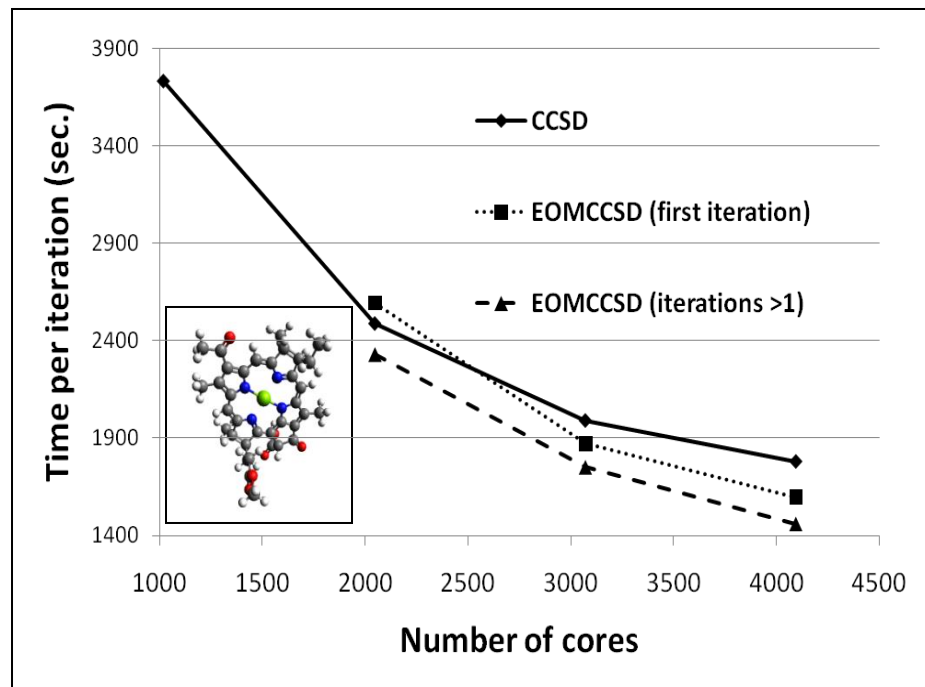
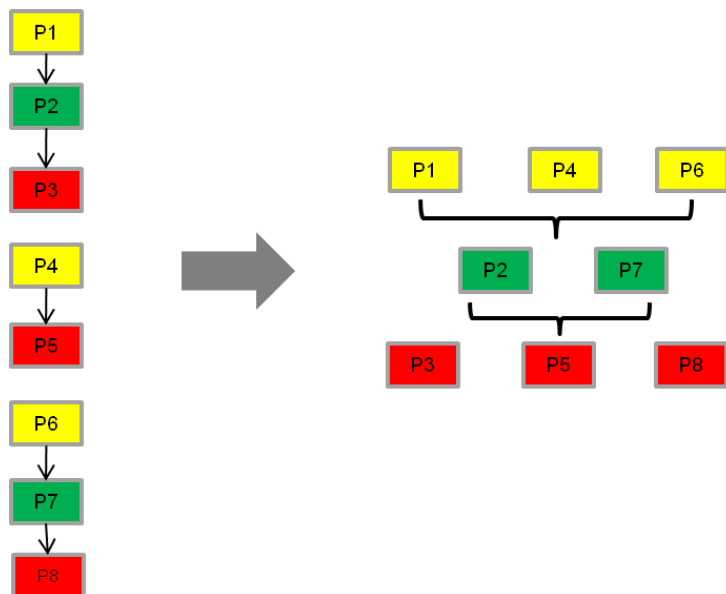
# New elements of parallel design for the iterative CCSD/EOMCCSD method



- Use of Global Arrays (GA) to implement a distributed memory model
- Iterative CCSD/EOMCCSD methods (basic challenges)
  - ◆ Global memory requirements
  - ◆ Complex load balancing
  - ◆ Complicated communication pattern: use of one-sided `ga_get`, `ga_put`, `ga_acc`
- Implementation improvements
  - ◆ New way of representing antisymmetric 2-electron integrals for the restricted (RHF) and restricted open-shell (ROHF) references
  - ◆ Replication of low-rank tensors
  - ◆ New task scheduling for the CCSD/EOMCCSD methods

# Scalability of the iterative EOMCC methods

- Alternative task schedulers
  - use “global task pool”
  - improve load balancing
  - reduce the number of synchronization steps to absolute minimum
  - larger tiles can be effectively used



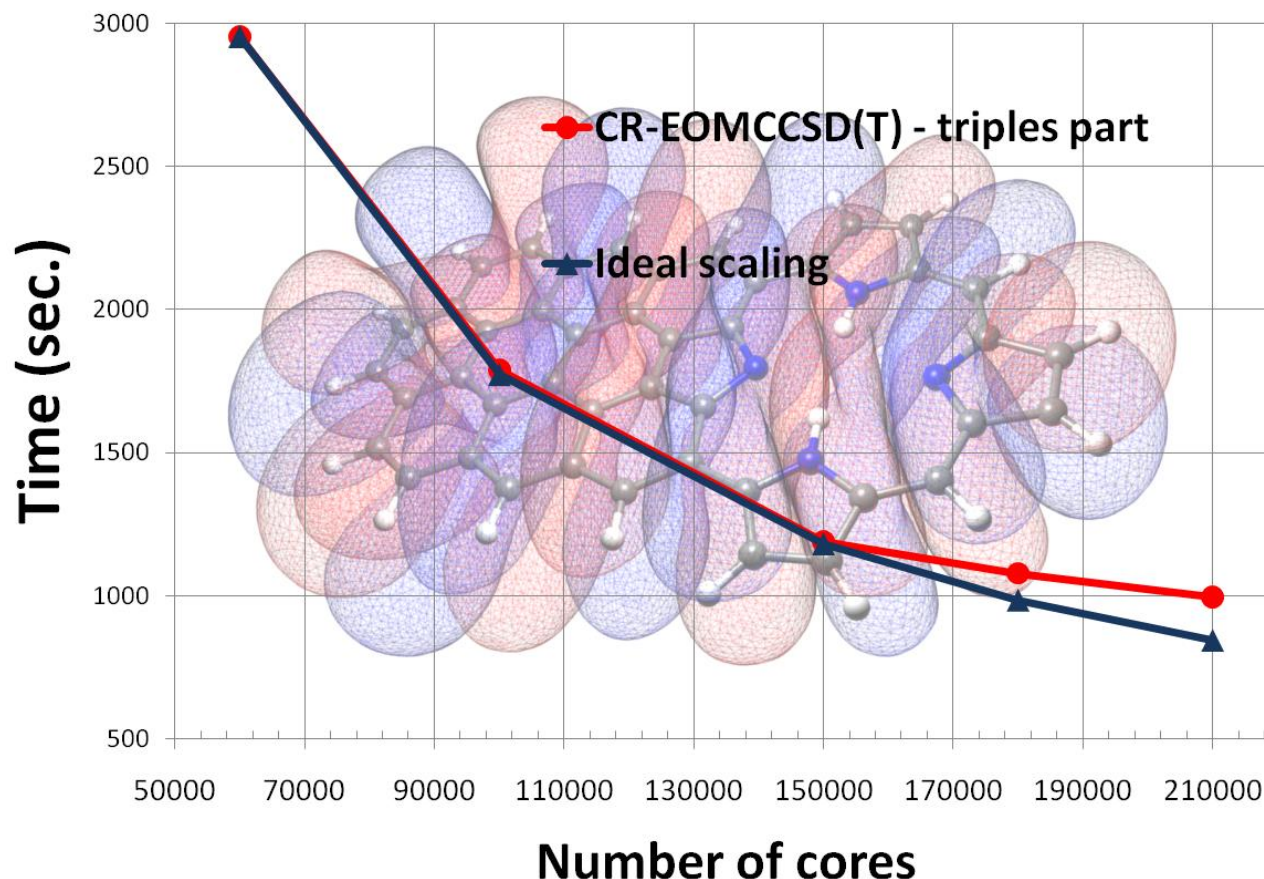
LAYER 1

LAYER 2

LAYER 3

- Use of Global Arrays (GA) to implement a distributed memory model
- Basic challenges for Non-Iterative CR-EOMCCSD(T) method
  - ◆ Local memory requirements:  $(\text{tile size})^4$  (EOMCCSD) vs.  $M^*(\text{tile size})^6$  (CR-EOMCCSD(T))
- Implementation improvements
  - ◆ Two-fold reduction of local memory use :  $2^*(\text{tile size})^6$
  - ◆ New algorithms which enable the decomposition of six-dimensional tensors

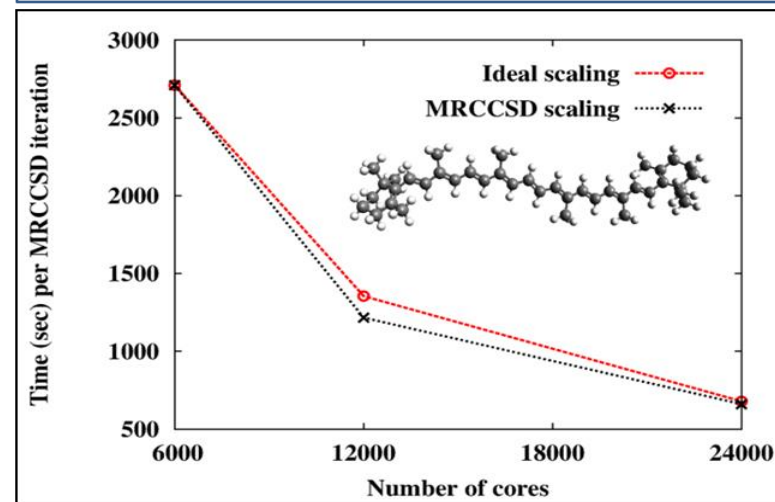
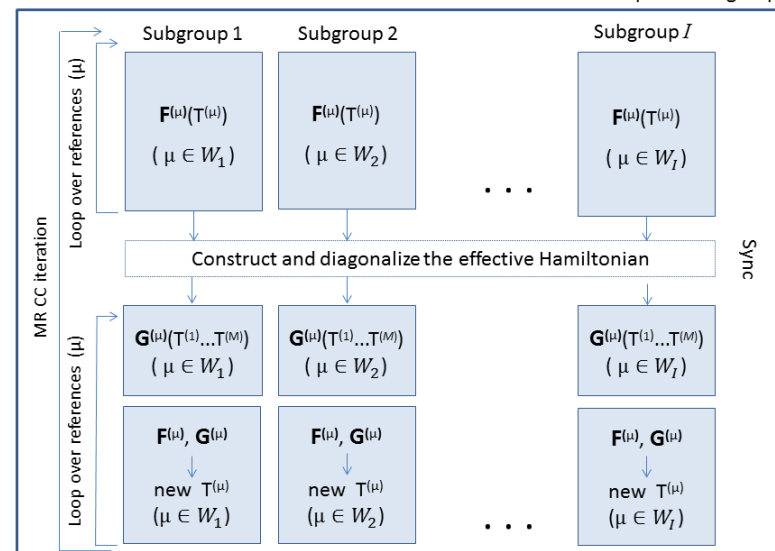
## 94 % parallel efficiency using 210,000 cores



Scalability of the triples part of the CR- EOMCCSD(T) approach for the FBP-f-coronene system in the AVTZ basis set. Timings were determined from calculations on the Jaguar Cray XT5 computer system at NCCS.

## Multireference CC methods in NWChem (next release)

- ◆ Strongly correlated excited states
- ◆ Implemented MRCC approaches
  - Brillouin-Wigner MRCCSD
  - Mukherjee Mk-MRCCSD approach
  - State-Universal MRCCSD (under testing)
  - Perturbative triples corrections MRCCSD(T)
- ◆ Novel parallelization strategies based on the processor groups
- ◆ Demonstrated scalability of MRCCSD across 24,000 cores



# Multireference CC methods

- Improve the quality of the MRCCSD approaches
- Counteract the intruder-state problem

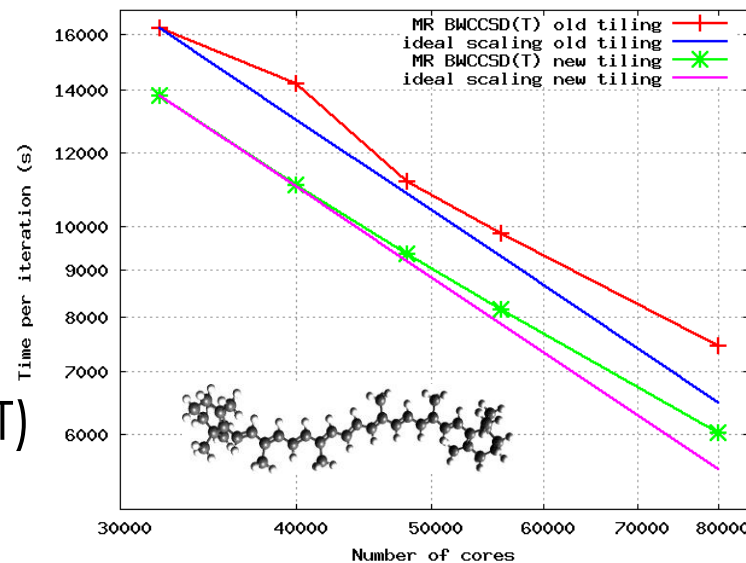
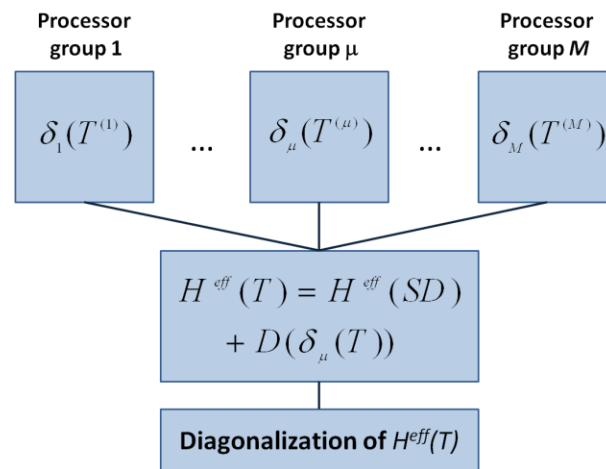
$$H_{\mu\mu}^{eff}(T) = H_{\mu\mu}^{eff}(SD) + \delta_{\mu}(T^{(\mu)})$$



Numerical complexity  $\sim M \times N^7$

Scalability  $\sim M \times (\text{scalability of the CCSD}(T) \text{ approach})$

**GPU** implementations of the MRCCSD(T) approaches are currently tested



K. Bhaskaran-Nair, J. Brabec, J. Pittner, H.J.J. van Dam, E. Apra, K. Kowalski, JCP (accepted).

# Questions?

